

CECÍLIA ROMARO

**ESTUDOS EM MODELOS DE REDES CORTICAIS
STUDIES IN CORTICAL NETWORK MODELS**

Ribeirão Preto
2020

CECÍLIA ROMARO

**ESTUDOS EM MODELOS DE REDES CORTICAIS
STUDIES IN CORTICAL NETWORK MODELS**

Tese apresentada à Faculdade de Filosofia
Ciências e Letras de Ribeirão Preto da Univer-
sidade de São Paulo para obtenção do Título
de Doutor em Ciências.

Ribeirão Preto
2020

CECÍLIA ROMARO

**ESTUDOS EM MODELOS DE REDES CORTICAIS
STUDIES IN CORTICAL NETWORK MODELS**

Tese apresentada à Faculdade de Filosofia
Ciências e Letras de Ribeirão Preto da Univer-
sidade de São Paulo para obtenção do Título
de Doutor em Ciências.

Área de Concentração:

Física Aplicada à Medicina e Biologia

Orientador:

Antônio Carlos Roque da Silva Filho

Co-orientador:

José Roberto Castilho Piqueira

Ribeirão Preto
2020

Romaro, Cecília

Studies in Cortical Network Models. Ribeirão Preto, 2020.
178 p. : il. ; 30 cm

Tese de Doutorado apresentada à Faculdade de
Filosofia, Ciências e Letras de Ribeirão Preto / USP. Área
de concentração: Física Aplicada à Medicina e Biologia.

Orientador: Roque da Silva Filho, Antônio Carlos

Co-orientador: Castilho Piqueira, José Roberto.

1. Somatosensory cortex model. 2. Mean-field potential.
3. Metastability behavior. 4. Rescaling neuron network.
5. Phase transition.

I dedicate this work to all people
who, in some way, act for a better
world.

ACKNOWLEDGMENTS

The author is the recipient of PhD scholarships from the Brazilian Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES, grant number 88882.378774/2019-01).

The author is thankful to NeuroMat for the scientific and stimulating environment; Professor Piqueira, who had a contribution in completion of this work beyond his imagination; her friend, “academic and life assistant” Angela, for always telling her the truth; her friend and “husband” Julia Maria, who stood by her side through parties and tears; and the author’s sister, “big little” Cinthia, for actually being her sister.

“I’m late! I’m late! For a very important date! No time to say hello, goodbye! I’m late! I’m late! I’m late!”

--White Rabbit (Alice in Wonderland)

RESUMO

Esta tese apresenta-se em cinco capítulos-artigos resolvendo de forma simples problemas e perguntas não triviais na neurociência computacional.

O primeiro capítulo apresenta uma reimplementação do modelo de Potjans-Diesmann (PD) para a microcircuitaria cortical local e uma técnica de redimensionamento do número de neurônios do modelo capaz de manter as probabilidades de conexões e o comportamento da atividade da rede mesmo quando redimensionada para 1% do tamanho original.

O segundo capítulo, baseado no potencial de campo médio, explica formalmente o método de redimensionamento e apresenta um novo método de corrigir e compensar a atividade dos neurônios da borda em redes com extensão espacial sem introduzir conexões toroidais e/ou oscilações.

O terceiro capítulo introduz extensão espacial ao modelo PD, soluciona o problema de borda e estuda a resolução espacial (topográfica) da atividade da rede como um reflexo da resolução estrutural.

O quarto capítulo, baseado em transição de fase e metaestabilidade, inovadoramente estuda o falso estado estacionário e o tempo de duração da atividade em redes que não recebem entrada externa forçada capaz de mantê-las ativas.

O quinto capítulo contém a caracterização da rede de neurônios do córtex somatossensorial primário do rato em termos do levantamento estatístico dos parâmetros. Em seguida, um modelo do córtex somatossensorial utilizando o neurônio estocástico de Galves-Löcherbach (GL) é construído com base nos parâmetros levantados. No fim do capítulo, apresenta-se um método para substituição de neurônios determinísticos do tipo integra-e-dispara com vazamento por neurônios GL em modelos de redes de neurônios.

Palavras-Chave – modelagem do córtex somatossensorial, potencial de campo médio, metaestabilidade, redimensionamento de rede neuronal, transição de fase.

ABSTRACT

This thesis consists of five chapter-articles, each proposing simple solutions to nontrivial questions and problems in computational neuroscience.

The first chapter presents a reimplementation of the Potjans-Diesmann (PD) model of the local cortical microcircuitry, and a rescaling method for the number of neurons in the model that is capable of maintaining both the connection probabilities and the behavior of the network activity even when rescaled to 1 % of original size.

The second chapter, based on mean field potential, formally explains the scaling method and presents a new method to correct and compensate for the activity of boundary neurons in networks with spatial extension without introducing toroidal connections and/or oscillations.

The third chapter introduces spatial extension to the PD model, solves the boundary problem, and studies the spatial (topographic) resolution of the network activity as a consequence of the structural resolution.

The fourth chapter, based on phase transition and meta-stability, innovatively studies the false steady state and activity lifetime in networks that do not receive forced external input to keep them active.

The fifth chapter contains a characterization of the primary somatosensory cortex network of the rat in terms of a statistical survey of the parameters. It also presents a model of the somatosensory cortex using the stochastic Galves-Löcherbach (GL) neuron, which was constructed based on the somatotopic parameters raised. At the end of the chapter, a method for replacing deterministic leaky integrate-and-fire neurons by GL neurons in neural network models is presented.

Keywords – somatosensory cortex model, mean-field potential, metastability behavior, rescaling neuron network, phase transition.

INTRODUCTION

Understanding the brain is challenging, given both its complex mechanisms and inaccessibility. Every year new pathways, channels, proteins, and other mechanisms are discovered, but how these components interact at the system level remains a mystery (Markram et al., 2015; Yin and Wang, 2016; Lisman and Raghavachari, 2006; Diekmann et al., 2013; Antunes et al., 2016). A strong mathematical research line appeared in the early XX century to explain the neuron behavior. The Hodgkin-Huxley (HH) (Hodgkin et al., 1952) and leaky integrate-and-fire (LIF) (Lapicque, 1907) models are some of the most classic and oldest mathematical models of neurons, and pools of these neurons were put together in attempts to study their collective behavior. However, it was only with the advancement of computational resources that the study of neuron networks was able to develop further (De Schutter, 2008). *In silico* simulation studies started to provide a quantitative framework for integrating disparate pieces of evidence from *in vivo* and *in vitro* experiments into coherent predictive models that can be used to investigate brain function.

Biologically detailed computational modeling became an excellent research tool to explain brain mechanisms and to propose supporting experiments *in vivo* (Markram et al., 2015; Mazza et al., 2004; Bower and Beeman, 2012). At the same time, simplified neurons became a study subject to understand the dynamics of neuron networks (Galves and Löcherbach, 2013; Potjans and Diesmann, 2014a; Brunel, 2000). These techniques are being largely adopted by research groups worldwide such as the Allen Institute for Brain Science (AIBS) (Jones et al., 2009) (<https://alleninstitute.org/what-we-do/brain-science/>), the Human Brain Project (HBP) (Markram, 2012) (<https://www.humanbrainproject.eu/en/>), the NEST initiative (Gewaltig and Diesmann, 2007) (<https://nest-initiative.org/>), and the Research, Innovation and Dissemination Center for Neuromathematics (NeuroMat) (<https://neuromat.numec.prp.usp.br/>). In this scenario, three neural simulators stand out today:

The NEURON simulator (Carnevale and Hines, 2006) (<https://neuron.yale.edu/neuron/>) allows modeling of networks of neurons with detailed neuronal morphologies, and different ion channels and neurotransmitter receptors. Developed at Yale University, NEURON is the most widely used simulator of its type, both in university labs and large research groups, including AIBS and HBP. It is an excellent software for the construction and simulation of biologically-detailed neuron networks, although it requires a large amount of machine

processing time.

The NEST simulator (Morrison et al., 2005; Gewaltig and Diesmann, 2007) (<https://nest-simulator.org/>) allows modeling of large networks of simplified neurons. It does not allow the direct introduction of morphology, ion channels and neurotransmitter receptors, but allows parallel and distributed simulation inboard build up in order to save machine time.

The Brian simulator (Goodman and Brette, 2009) (<https://briansimulator.org/>) has inboard differential equation solvers and other facilities to simulate spiking neural networks. Brian is an easy install simulator, given it is a Python package. It is not as fast as NEST, but it is more plastic. Neither Brian nor NEST allow the direct introduction of morphology or physical characteristics of neurons.

Although great advancement has been achieved, it seems that computational resources still pose a limiting factor to simulate, process, and understand detailed models of large networks (Markram et al., 2015; Towns et al., 2014). This limit is being pushed further and further away as computational resources become more powerful and cheaper, and this both supports and inspires the work done in this thesis.

This thesis starts by presenting a re-implementation of the Potjans-Diesmann (PD) model (Potjans and Diesmann, 2014a) in NetPyNE/NEURON (Dura-Bernal et al., 2019b; Carnevale and Hines, 2006) (<http://www.netpyne.org/>), a high-level Python interface to the NEURON simulator. The PD model, originally implemented in NEST (Gewaltig and Diesmann, 2007), is an eight-cell population model which reproduces the neuronal connectivity under a 1 mm^2 area of cortical surface in full scale (the model has 77,169 neurons). The PD model generates spontaneous activity with population-specific firing rates similar to those observed experimentally (de Kock and Sakmann, 2009; Sakata and Harris, 2009; Swadlow, 1989). The re-implementation of the PD model in NetPyNE/NEURON allows the use of more detailed neuron models with multicompartmental morphologies and multiple realistic biophysical ion channels. Additionally, some analyses can be provided automatically.

Due to the required memory and processing power to re-implement the PD model in NEURON (Carnevale and Hines, 2006), a rescaling method was developed to scale down the model to variable levels, down to the lowest level of 1%. The method allows to decrease the number of connections to 10^{-4} of the original number still maintaining characteristics of network activity behavior compatible with experimental data: mean population firing rate, synchrony and irregularity (Romaro et al., 2018, 2020a).

The re-scaling method introduced here can be applied not only to the PD model but to random neuron network models in general, e.g. the Brunel model (Brunel, 2000). This method

is further explored in chapter 2, and both a detailed mathematical explanation based on mean field potential and a list of the method limitations are presented there. Based on the re-scaling method, networks with spatial extension are considered in chapter 2 and a boundary solution method is introduced. The boundary solution method is able to correct and compensate the lack (or excess) of connections at the boundary in order to reestablish the correct activity of boundary-neurons and core-neurons.

The boundary solution method was developed because it was needed in the construction of a model of the primary somatosensory cortex exhibiting somatotopy, the main subject of Chapter 3.

Somatotopy is the topographic organization of somatic sensory pathways – touch and proprioception – in the primary somatosensory cortex (S1, located in the post-central gyrus) (Bear et al., 2020). That is, the mapping of neighboring areas of the skin to neighboring areas in the cortex, e.g. two sensors in the skin close together activate in the cortex two groups of neurons that are close together. Many models have been proposed to reproduce and explain the mechanisms and effects of the topographic organization in S1, including the re-organization properties following some lesion (Ramachandran, 1998; Bear et al., 2020). A property of the somatotopic maps is the direct proportionality between the cortical area allocated to represent a body surface and the sensitivity of this surface. In other words, the higher the sensitivity of a body area, the higher the cortical area allocated to process it (Bear et al., 2020). However, none of these models explored the influence of the connectome on the resolution of the topographic map in S1.

In chapter 3, adjustments are introduced in the PD model in order to adapt it to describe the somatosensory cortex and allow a study of the role of network structure and activity on the topographic organization and spatial resolution of inputs. These adjustments include the introduction of spatial locations for the neurons and consideration of distance-dependent connectivity to integrate anatomical and physiological data. This leads to a model that accounts for the topographic pattern of connections. The objective is to shed some light on the question of how the parameters of the topographic connections relate to the local activity patterns in specific cortical layers.

Work on cortical network models raised other questions that were studied during the period of this doctorate and resulted in chapters 4 and 5.

One of these questions is how to characterize the lifetime of active states in a network in the absence of external input. In the context of the Galves-Löcherbach (GL) model (Galves and Löcherbach, 2013), André has recently proved (André, 2019b) that for finite one-dimensional

lattices of continuous GL neurons with hard threshold rate function (Ferrari et al., 2018), in the sub-critical regime where the leak rate γ is smaller than a critical value γ_c the lifetime of the active state is finite but the exit time from this state is exponentially distributed. In chapter 4, a computational version of the finite lattice model considered by André is described together with extensions of the model to two- and three-dimensional square lattices and linear and sigmoidal rate functions. The simulation studies confirm the rigorous results obtained by André and provide evidence that they also hold in the extended settings considered (Romaro et al., 2019).

Another question is related to the common practice of using data from a mix of different cortical areas and animals in the construction of a model for a specific cortical area from a given animal. For example, the PD model uses data from the primary somatosensory, motor and visual cortices of rat and rabbit (Potjans and Diesmann, 2014a). To address this problem, in chapter 5 a statistical survey of parameters from the connectome of the primary somatosensory cortex of the rat is made. This allowed the construction of a model of the primary somatosensory cortex of the rat with GL neurons.

References are presented at the end of each chapter, except for introduction references, which are presented in the References section. Chapter 1 was developed in collaboration with Fernando Najman and Salvador Dura-Bernal. Chapter 4 was developed in collaboration with Fernando Najman and Morgan Andre.

CONCLUSION

This thesis focused on modeling neuronal networks and some mathematical tools and properties needed to do so.

The thesis proposed new approaches to known, yet limited, topics such as rescaling the network size while maintaining the first and second order statistics with the objective of decreasing machine time or increasing network details, and solving the boundary problem without loss of activity for spatially extended networks with topographic pattern of connections (Chapters 1 and 2).

A correlation between spatial resolution in activity and the standard deviation of the Gaussian distribution was utilized to propose a scheme for the construction of a network with topographic pattern of connections. This is the subject of Chapter 3.

The thesis also shows that the metastable phase transition depends on the spike-waste rate, and not on the network connectivity pattern (Chapter 4).

Lastly, the thesis presented a network model for the primary somatosensory cortex based on the GL stochastic neuron (Galves and Löcherbach, 2013). The network model was able to reproduce the biological average firing rate per layer, self-sustained activity without external input, and two activity states and the shift between them by a one-step interference in Layers L4e and L5e. This network also presented asynchronous activity and neurons with regular and irregular behaviour inside the same layer.

WORKS RESULTING FROM THIS THESIS

Articles submitted or placed in ArXiv

Romaro, C., Najman, F. A., Lytton, W. W., Roque, A. C., and Dura-Bernal, S. (2020). NetPyNE implementation and rescaling of the Potjans-Diesmann cortical microcircuit model. arXiv preprint arXiv:2005.03764. (Neural Computation)

Romaro, C., Najman, F. A., and André, M. (2019). A Numerical Study of the Time of Extinction in a Class of Systems of Spiking Neurons. arXiv preprint arXiv:1911.02609. (Journal of Statistical Physics)

Romaro, C., Roque, A. C., and Piqueira, J. R. C. (2020). Boundary solution based on rescaling method: recoup the first and second-order statistics of neuron network dynamics. arXiv preprint arXiv:2002.02381

Articles in preparation

Somatotopic organization in the cell-type specific cortical microcircuit and input spacial resolution. (Chapter 3)

Specific cortical microcircuit model based on somatosensory cortex connectome of juvenile rat. (Chapter 5)

Conference abstracts

Compensating method for the lack of connection on topographic neuron network edge (Submitted to CNS*2020)

Romaro, C., Najman, F. A., and André, M. (2019). Dynamical phase transitions study in simulations of finite neurons network. (In: Bojak, I. and Nowotny, T., eds. (2019) 28th Annual Computational Neuroscience Meeting: CNS*2019. BMC Neuroscience, pp190. doi: <https://doi.org/10.1186/s12868-019-0538-0> Available at <http://centaur.reading.ac.uk/88633/>)

Romaro, C., Najman, F., Dura-Bernal, S., and Roque, A. C. (2018). Implementation of the Potjans-Diesmann cortical microcircuit model in NetPyNE/NEURON with rescaling option.

BMC Neuroscience, (64), sup-2. **This work won the Best Poster Award** (In: 27th Annual Computational Neuroscience Meeting (CNS*2018): Part One. BMC Neurosci 19, 64 (2018). <https://doi.org/10.1186/s12868-018-0452-x>)

Romaro, C., Roque, A. C. (2017). Network model of the primary somatosensory cortex: a study of the connection pattern. SBNeC (2018). (In: XL SBNeC - Brazilian Society of Neurosciences and Behavior. (Presentation) UNESP – São Paulo State University, Santos, SP, Brazil.)

Romaro, C., Shimoura, R. O., Roque, A. C. (2017). Somatotopic representation in microcircuitry modeling of the mammalian cortex. (In: XL SBNeC - Brazilian Society of Neurosciences and Behavior. (Presentation) UNESP – São Paulo State University, Araraquara, SP, Brazil.)

Romaro, C., Shimoura, R. O., Kamiji, N. L., Roque, A. C. (2017). Reorganização somatotópica em um modelo de microcircuito local do córtex de mamífero. (In: XXII CBFM - Brazilian Congress of Medical Physics, 3399.)

REFERENCES

- André, M. (2019b). A result of metastability for an infinite system of spiking neuron. *Journal of Statistical Physics*, 177:984–1008.
- Antunes, G., Roque, A. C., and De Souza, F. M. S. (2016). Modelling intracellular competition for calcium: kinetic and thermodynamic control of different molecular modes of signal decoding. *Scientific Reports*, 6:23730.
- Bear, M., Connors, B., and Paradiso, M. A. (2020). *Neuroscience: Exploring the brain*. Jones & Bartlett Learning, LLC.
- Bower, J. M. and Beeman, D. (2012). *The book of GENESIS: exploring realistic neural models with the GEneral NEural Simulation System*. Springer Science & Business Media.
- Brunel, N. (2000). Dynamics of sparsely connected networks of excitatory and inhibitory spiking neurons. *Journal of Computational Neuroscience*, 8(3):183–208.
- Carnevale, N. T. and Hines, M. L. (2006). *The NEURON Book*. Cambridge University Press.
- de Kock, C. P. and Sakmann, B. (2009). Spiking in primary somatosensory cortex during natural whisking in awake head-restrained rats is cell-type specific. *Proceedings of the National Academy of Sciences (USA)*, 106(38):16446–16450.
- De Schutter, E. (2008). Why are computational neuroscience and systems biology so separate? *PLoS Computational Biology*, 4(5):e1000078.
- Diekman, C. O., Fall, C. P., Lechleiter, J. D., and Terman, D. (2013). Modeling the neuroprotective role of enhanced astrocyte mitochondrial metabolism during stroke. *Biophysical Journal*, 104(8):1752–1763.
- Dura-Bernal, S., Suter, B. A., Gleeson, P., Cantarelli, M., Quintana, A., Rodriguez, F., Kedziora, D. J., Chadderdon, G. L., Kerr, C. C., Neymotin, S. A., et al. (2019b). Netpyne, a tool for data-driven multiscale modeling of brain circuits. *Elife*, 8:e44494.
- Ferrari, P., Galves, A., Grigorescu, I., and Löcherbach, E. (2018). Phase transition for infinite systems of spiking neurons. *Journal of Statistical Physics*, 172(6):1564–1575.

- Galves, A. and Löcherbach, E. (2013). Infinite systems of interacting chains with memory of variable length—a stochastic model for biological neural nets. *Journal of Statistical Physics*, 151(5):896–921.
- Gewaltig, M.-O. and Diesmann, M. (2007). NEST (neural simulation tool). *Scholarpedia*, 2(4):1430.
- Goodman, D. F. and Brette, R. (2009). The brian simulator. *Frontiers in Neuroscience*, 3:26.
- Hodgkin, A. L., Huxley, A. F., and Katz, B. (1952). Measurement of current-voltage relations in the membrane of the giant axon of loligo. *Journal of Physiology*, 116(4):424–448.
- Jones, A. R., Overly, C. C., and Sunkin, S. M. (2009). The allen brain atlas: 5 years and beyond. *Nature Reviews Neuroscience*, 10(11):821–828.
- Lapicque, L. (1907). Recherches quantitatives sur l’excitation électrique des nerfs traitée comme une polarisation. *Journal de Physiologie et de Pathologie Generale*, 9:620–635.
- Lisman, J. and Raghavachari, S. (2006). A unified model of the presynaptic and postsynaptic changes during ltp at cal synapses. *Science’s STKE*, 2006(356):re11–re11.
- Markram, H. (2012). The human brain project. *Scientific American*, 306(6):50–55.
- Markram, H., Muller, E., Ramaswamy, S., Reimann, M. W., Abdellah, M., Sanchez, C. A., Ailamaki, A., Alonso-Nanclares, L., Antille, N., Arsever, S., et al. (2015). Reconstruction and simulation of neocortical microcircuitry. *Cell*, 163(2):456–492.
- Mazza, M., De Pinho, M., Piqueira, J. R. C., and Roque, A. C. (2004). A dynamical model of fast cortical reorganization. *Journal of Computational Neuroscience*, 16(2):177–201.
- Morrison, A., Mehring, C., Geisel, T., Aertsen, A., and Diesmann, M. (2005). Advancing the boundaries of high-connectivity network simulation with distributed computing. *Neural Computation*, 17:1776–1801.
- Potjans, T. C. and Diesmann, M. (2014a). The cell-type specific cortical microcircuit: relating structure and activity in a full-scale spiking network model. *Cerebral Cortex*, 24(3):785–806.
- Ramachandran, V. S. (1998). Consciousness and body image: lessons from phantom limbs, capgras syndrome and pain asymbolia. *Philosophical Transactions of the Royal Society of London. Series B: Biological Sciences*, 353(1377):1851–1859.

- Romaro, C., Najman, F., Dura-Bernal, S., and Roque, A. C. (2018). Implementation of the potjans-diesmann cortical microcircuit model in netpyne/neuron with rescaling option. *BMC Neuroscience*, (64):sup–2.
- Romaro, C., Najman, F. A., and André, M. (2019). A numerical study of the time of extinction in a class of systems of spiking neurons. *arXiv:1911.02609*.
- Romaro, C., Najman, F. A., Lytton, W. W., Roque, A. C., and Dura-Bernal, S. (2020a). Net-PyNE implementation and rescaling of the Potjans-Diesmann cortical microcircuit model. *arXiv:2005.03764*.
- Sakata, S. and Harris, K. D. (2009). Laminar structure of spontaneous and sensory-evoked population activity in auditory cortex. *Neuron*, 64(3):404–418.
- Swadlow, H. A. (1989). Efferent neurons and suspected interneurons in s-1 vibrissa cortex of the awake rabbit: receptive fields and axonal properties. *Journal of Neurophysiology*, 62(1):288–308.
- Towns, J., Cockerill, T., Dahan, M., Foster, I., Gaither, K., Grimshaw, A., Hazlewood, V., Lathrop, S., Lifka, D., Peterson, G. D., et al. (2014). Xsede: accelerating scientific discovery. *Computing in Science & Engineering*, 16(5):62–74.
- Yin, X. and Wang, R. (2016). The computational simulation of the effect of dopamine on short-term and long-term memory. In *Advances in Cognitive Neurodynamics (V)*, pages 645–652. Springer.